



FINAL TEST SERIES XI JEE TEST-01 ANSWER KEY

Test Date :19-01-2020

[PHYSICS]

1. Answer (2)

$$h = \frac{1}{2}gt^2 \quad \dots(1)$$

$$\frac{h}{2} = \frac{1}{2}g(t-1)^2 \quad \dots(2)$$

Solving, $t = 3.41$ sec.

2. Answer (3)

For equilibrium,

$$F = -\frac{dU}{dx} = 0 = \frac{d}{dx}(x^2 - 6x) = 2x - 6 \Rightarrow x = 3\text{ m}$$

At $x = 3$ m, $U = 9 - 18 = -9$ joule

$$E = K + U$$

$$11 = K + (-9) \Rightarrow K = 20 \text{ J}$$

3. Answer (2)

$$V_{\max} = \sqrt{gr \tan(\theta + \lambda)} = \sqrt{gr \frac{(\tan\theta + \tan\lambda)}{(1 - \tan\theta \cdot \tan\lambda)}}$$

$$= \sqrt{gr \frac{(\tan\theta + \mu)}{[1 - \tan\theta \times \mu]}} = \sqrt{\frac{10 \times 2 \left(\frac{3}{4} + \frac{1}{2}\right)}{\left(1 - \frac{1}{2} \times \frac{3}{4}\right)}}$$

$$= \sqrt{200 \times \frac{5 \times 8}{4 \times 5}} = \sqrt{400} = 20 \text{ ms}^{-1}$$

4. Answer (4)

$$x = 4t^2 - 3t \Rightarrow v = 8t - 3 \Rightarrow a = 8 \text{ ms}^{-2}$$

$$\Rightarrow \boxed{F = 16\text{N}} \Rightarrow dx = (8t - 3)dt$$

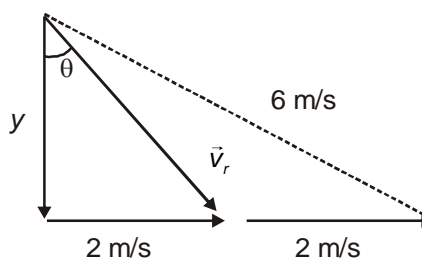
$$W = \int dW = \int Fdx = \int_0^t 16(8t - 3)dt = 16(4t^2 - 3t)$$

$$t = \frac{3}{4} \text{ s}, W = 0$$

$$\text{For } W \text{ to be minimum, } \frac{dW}{dt} = 0 \Rightarrow t = \frac{3}{8} \text{ s}$$

$$\frac{d^2W}{dt^2} = 8, \frac{d^2W}{dt^2} > 0$$

5. Answer (4)



$$\frac{2}{y} = \tan\theta$$

$$y = 2 \cot\theta$$

$$\text{Now, } \sqrt{y^2 + 16} = 36 \Rightarrow 4 \cot^2\theta + 16 = 36$$

$$\Rightarrow \cot^2\theta = 5 \Rightarrow \theta = \cot^{-1}(\sqrt{5})$$

6. Answer (2)

$$3kx_1 = 2kx_2 = kx_3 \Rightarrow 3x_1 = 2x_2 = x_3 \quad \dots(1)$$

$$x = x_1 + x_2 + x_3$$

$$\Rightarrow x = x_1 + \frac{3}{2}x_1 + 3x_1 \Rightarrow x = \frac{11x_1}{2}$$

$$\Rightarrow x_1 = \frac{2}{11}x.$$

7. Answer (1)

8. Answer (3)

$$2T - mg = ma_1 \uparrow \quad \dots(1)$$

$$Mg - T = Ma_2 \downarrow \quad \dots(2)$$

$$a_{\text{rel}} = a_1 + a_2 \quad \dots(3)$$

$$a_2 = 2a_1 \quad \dots(4)$$

$$\text{Solving, } a_1 = \frac{3g}{21}$$

Then $a_{rel} = \frac{3g}{21} + \frac{6g}{21} = \frac{9}{21}g = \frac{3g}{7}$

Now, $l = \frac{1}{2}a_{rel}.t^2 \Rightarrow l = \frac{1}{2} \times \frac{3g}{7}.t^2 \Rightarrow t = \sqrt{\frac{14g}{3l}}$

9. Answer (3)

$$\vec{v}_{rel} = (v - v \cos \theta)\hat{i} + v \sin \theta \hat{j} \Rightarrow |\vec{v}_{rel}|$$

$$= v\sqrt{(1 - \cos \theta)^2 + \sin^2 \theta} = 2v \sin \frac{\theta}{2}$$

$$|\vec{v}_{rel}| = \frac{\int_0^{2\pi} 2v \sin \theta / 2 d\theta}{2\pi \int_0^{2\pi} d\theta} = \frac{2v}{2\pi} = \frac{\left(-\cos \frac{\theta}{2}\right)_0^{2\pi}}{1} = \frac{1}{2}$$

$$= \frac{2v}{\pi} \left[-\cos \frac{\theta}{2}\right]_0^{2\pi} = \frac{4v}{\pi}$$

10. Answer (4)

For no motion between blocks,

$$F_{max} = \mu_2(m_1 + m_2)g = 0.4 \times 10 \times 10 = 40 \text{ N}$$

Thus, $F_{max} = 40 \text{ N}$

As, $F_{max} > F$ applied.

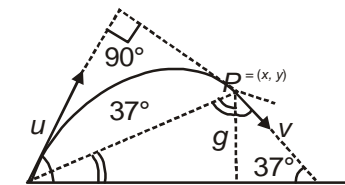
Hence between blocks $a_{rel} = 0$

$$\Rightarrow a_{common} = \frac{30}{10} = 3 \text{ ms}^{-2}$$

Now, for 4 kg

$$f = ma = 4 \times 3 = 12 \text{ N.}$$

11. Answer (3)



$$\theta = 53$$

When $\vec{v} \perp \vec{u}$

$$t = \frac{u}{g \sin \theta} \quad \dots(1)$$

$$v = u \cot \theta \quad \dots(2)$$

$$\Rightarrow v = u \times \frac{3}{4} = 10 \times \frac{3}{4} = \frac{15}{2} \text{ ms}^{-1}$$

$$\text{At P, } \frac{v^2}{R} = g \cos 37^\circ \Rightarrow R = \frac{v^2}{g \cos 37^\circ}$$

$$\Rightarrow R = \frac{15}{2} \times \frac{15}{2} \times \frac{5}{10 \times 4}$$

$$R = \frac{225}{32} \text{ m}$$

12. Answer (4)

$$F_{\text{upon}} \text{ due to } B = (m_A + m_B)(g + a)$$

$$= (2 + 3)(10 + 2) = 60 \text{ N} \downarrow$$

$$\text{Displacement } s = ut + \frac{1}{2}at^2 = -5 \times t = \frac{1}{2} \times 2 \times t^2$$

$$= -5 \times 2 + \frac{1}{2} \times 2 \times 4 = -10 + 4 = 6 \text{ m} \downarrow$$

$$W = \vec{F} \cdot \vec{S} = 60 \times 6 = 360 \text{ J}$$

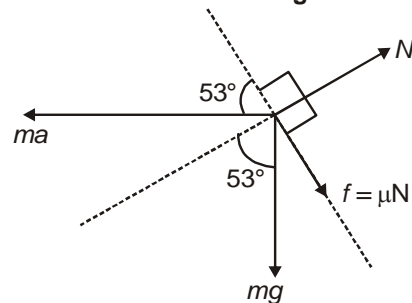
13. Answer (3)

$$N = mg \cos 53^\circ + ma \sin 53^\circ$$

$$N = mg \times \frac{3}{5} + ma \times \frac{4}{5} \quad \dots(1)$$

$$\mu N + mg \sin 53^\circ = ma \cos 53^\circ \quad \dots(2)$$

FBD of block w.r.t. wedge



$$0.1 \left[\frac{3}{5} mg + \frac{4}{5} ma \right] + \frac{4}{5} mg = \frac{3}{5} ma$$

$$\frac{1}{10} [3mg + 4ma] + 4mg = 3ma$$

$$3mg + 4ma + 40mg = 30ma$$

$$\Rightarrow 43mg = 26ma$$

$$\Rightarrow a = \frac{43}{26}g \quad \dots(3)$$

$$\text{Now, } F = (M + m)a = 6 \times \frac{43}{26}g = \frac{129}{13} \text{ g N}$$

14. Answer (1)

$$T - mg = ma \quad \dots(1)$$

$$Mg - 31T = M \times \frac{a}{31} \quad \dots(2)$$

$$\text{Solving, } a = \frac{31g(M - 31m)}{M + 961m}$$

15. Answer (4)

From work-energy theorem,

$$W_F + W_{by} mg + W_{by} tr = \Delta K = 0$$

$$W_F - mgR \sin 60^\circ - \mu mg(R - R \cos 60^\circ) = 0$$

$$W_F = mgR \frac{\sqrt{3}}{2} + \frac{\mu mgR}{2} = \frac{mgR}{2} (\mu + \sqrt{3})$$

16. Answer (3)

$$F = -\frac{dU}{dx} = -\left[\frac{d}{dx} \left(-\frac{2}{3}x^3 + \frac{3}{2}x^2 + 2x \right) \right]$$

$$= -\left[-\frac{2}{3} \times 3x^2 + \frac{3}{2} \times 2x + 2 \right] = -[-2x^2 + 3x + 2]$$

$$F = 2x^2 - 3x - 2 \quad \dots(1)$$

$$F = 0 \Rightarrow 2x^2 - 3x - 2 = 0$$

$$\Rightarrow 2x^2 - 4x + x - 2 = 0$$

$$\Rightarrow 2x(x - 2) + 1(x - 2) = 0$$

$$x = 2, \quad x = -\frac{1}{2}$$

$$\text{Now, } \frac{dF}{dx} = 4x - 3 \text{ at } x = 2,$$

$$\frac{dF}{dx} = 4 \times 2 - 3 = 8 - 3 = 5$$

$$\frac{dF}{dx} > 0 \Rightarrow \frac{d^2y}{dx^2} < 0$$

Thus at $x = 2$, unstable equilibrium.

$$\text{At } x = -\frac{1}{2}, \frac{dF}{dx} = 4x \left(-\frac{1}{2} \right) - 3x = -5, \frac{dF}{dx} < 0$$

$$\Rightarrow \frac{d^2y}{dx^2} > 0$$

Thus $x = -\frac{1}{2}$, stable equilibrium.

17. Answer (4)

Limiting friction between B and $C = 0.5 \times 4 \times 10 = 20 \text{ N}$

$$\text{Maximum common acceleration} = \frac{20}{4} = 5 \text{ ms}^{-2}$$

$$\text{Now, } a_{\max} = \frac{m_{A\max} \cdot g}{m_A + 3 + 4} \Rightarrow 5 = \frac{m \times 10}{m + 7}$$

$$10m_A = 5m_A + 35 \Rightarrow m_A = 7 \text{ kg}$$

$$\text{When } m_A = 5 \text{ kg, } a = \frac{5 \times 10}{5 + 3 + 4} = \frac{50}{12} \text{ ms}^{-2}$$

$$\Rightarrow f = 4 \times \frac{50}{12} = \frac{50}{3} \text{ N}$$

18. Answer (4)

$$\text{At } A, T_A - mg = \frac{mv_A^2}{l} \Rightarrow T_A = mg + 6mg = 7mg$$

$$\text{At } B, T_B = \frac{mv_B^2}{l} = 4mg, T \text{ and } C,$$

$$T_C + mg - \frac{mv_C^2}{l} \Rightarrow T_C = m \times \frac{V_C^2}{l} - mg - 2mg - mg$$

$$\boxed{T_B = 4mg} \quad \boxed{T_A = 7mg} \quad \boxed{T_C = mg}$$

19. Answer (4)

$$\text{For UCM, } \vec{v} \perp \frac{d}{dt} \vec{v}$$

$$\text{For accelerated CM, } \vec{v} \cdot \frac{d}{dt} \vec{v} > 0$$

$$\text{For decelerated CM, } \vec{v} \cdot \frac{d}{dt} \vec{v} < 0.$$

20. (b) $\therefore E = \frac{1}{2}mv^2$
 \therefore % Error in K.E.
 = % error in mass + 2 × % error in velocity
 = 2 + 2 × 3 = 8 %

21. $200 - 120 = 12a_1 \Rightarrow a_1 = \frac{80}{12} = \frac{20}{3} \text{ms}^{-2} \uparrow$

$200 - 150 = 15a_2 \Rightarrow a_2 = \frac{50}{15} = \frac{10}{3} \text{ms}^{-2} \uparrow$

$$a_p = \frac{\frac{20}{3} + \frac{10}{3}}{2} = 5 \text{ms}^{-2} \uparrow$$

22. Answer (4)

$$F = -\frac{dU}{dx} \Rightarrow \frac{dU}{dx} = -F$$

$$\Rightarrow \text{For equilibrium, } F = 0 \Rightarrow \frac{dU}{dx} = 0$$

For stable equilibrium,

$$\frac{d^2U}{dx^2} > 0 \Rightarrow \frac{d}{dx} \left(\frac{dU}{dx} \right) > 0 \Rightarrow \frac{d}{dx}(-F) > 0 \Rightarrow -\frac{dF}{dx} > 0$$

$$\Rightarrow \frac{dF}{dx} < 0 \text{ for unstable equilibrium, } \frac{dF}{dx} > 1.$$

23. Answer (2)

$$2.221$$

$$\times 1.2$$

$$\frac{2.6652}{2} = 2.7$$

Now,

$$238.523$$

$$2.7$$

$$241.2$$

Number of SF = 4

24. Answer (2)

$$t = \frac{s_{\text{rel}}}{v_{\text{rel}}} = \frac{l}{v + v \cos 60^\circ} = \frac{2l}{3v}$$

$$\text{Distance} = v \times t = v \times \frac{2l}{3v} = \frac{2l}{3} = \frac{2}{3} \times 3 = 2 \text{ m.}$$

25. Answer (4)

$$\mu_s mg = m \sqrt{a_T^2 + \frac{v_m^4}{r^2}}$$

$$\Rightarrow \mu^2 g^2 = a_T^2 + \frac{v_m^4}{r^2}$$

$$\Rightarrow \frac{1}{4} \times 100 = 9 + \frac{v_m^4}{16}$$

$$\Rightarrow v_m^4 = 16 \times 16$$

$$\Rightarrow v_m = 4 \text{ms}^{-1}$$

$$\text{Now, } a = \frac{vdv}{ds} \Rightarrow vdv = ads$$

$$\int_u^v vdv = \int_0^s ads$$

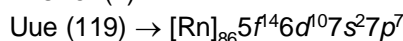
$$v^2 = u^2 + 2as$$

$$(4)^2 = (2)^2 + 2 \times 3 \times s$$

$$2 \times 6 = 6 \times s \Rightarrow \boxed{s = 2\text{m}}$$

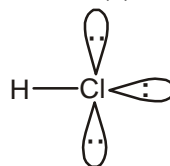
[CHEMISTRY]

26. Answer (1)



Hence it belongs to 17th group.

27. Answer (3)



1 bond pair, 3 lone pair.

28. Answer (1)

NO (15) Bond order = 2.5

NO⁺ (14) Bond order = 3

NO⁻ (16) Bond order = 2

Hence, order of bond energy NO⁺ > NO > NO⁻

29. Answer (2)

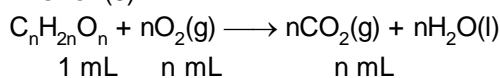
Let the uncertainty in momentum = x

Uncertainty in position = 4x

$$\therefore 4x^2 = \frac{h}{4\pi} \Rightarrow x = \frac{1}{4} \sqrt{\frac{h}{\pi}}$$

Hence uncertainty in position = $\sqrt{\frac{h}{\pi}}$.

30. Answer (3)



$$1 \text{ mL} \quad n \text{ mL} \quad \quad n \text{ mL}$$

\therefore Contraction in volume = 1 + n - n = 1 mL.

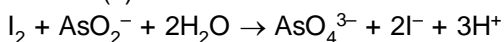
31. Answer (4)

Fact.

32. Answer (2)

Electronic configuration (56) – $[\text{Xe}]_{54}6s^2$

33. Answer (1)



m.eq. of HAsO_2 (in 50 mL) = m.eq. of $\text{I}_2 = 35 \times 0.05 \times 2 = 3.5$

\therefore meq of HAsO_2 in 250 mL = 17.5

$$\text{weight of } \text{HAsO}_2 = \frac{17.5}{2} \times 108 \times 10^{-3} = 0.945 \text{ g}$$

$$\% \text{ of } \text{HAsO}_2 \text{ in the sample} = \frac{0.945}{3.78} \times 100 = 25\%$$

34. Answer (3)

Isodiaphers have same (n - p)

35. Answer (4)

 XeOF_4 is square pyramidal.

36. Answer (2)

C : H : N = 9 : 1 : 3.5

Ratio by moles

$$\text{C} : \text{H} : \text{N} = \frac{9}{12} : \frac{1}{1} : \frac{3.5}{14} = \frac{3}{4} : 1 : 1 : \frac{1}{4} = 3 : 4 : 1$$

 $\text{C}_3\text{H}_4\text{N}$ is empirical formula.

$$n = \frac{108}{54} = 2$$

Hence molecular formula $\text{C}_6\text{H}_8\text{N}_2$

37. Answer (3)

Separation energy

$$= 13.6 \times \frac{Z^2}{n^2} = 13.6 \times \frac{3^2}{2^2} = +30.6$$

(\therefore for first excited state $n = 2$)

38. Answer (3)

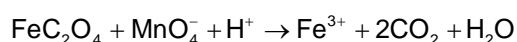
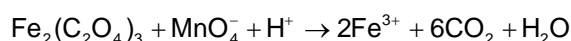
39. Answer (2)

$$2\pi r_n = n\lambda \Rightarrow 2\pi \times 0.53 \frac{n^2}{Z} = n\lambda$$

$$\Rightarrow \lambda = 2\pi \times 0.53 \times \frac{n}{Z}$$

$$E_{\text{sep}} = 3.4 = 13.6 \frac{Z^2}{n^2} \Rightarrow \frac{n}{Z} = 2$$

40. Answer (2)

Total equivalents of $\text{Fe}_2(\text{C}_2\text{O}_4)_3$ and FeC_2O_4 = equivalents of KMnO_4 On solving, $x = 0.9$ mole.

41. Answer (3)

Limiting agent is Na_2CO_3 .Now 106 g of Na_2CO_3 gives 22.4 L of CO_2

$$\therefore 5.3 \text{ g of } \text{Na}_2\text{CO}_3 \text{ gives } \frac{22.4}{106} \times 5.3 = 1.12 \text{ L}$$

42. Answer (4)

Fact.

43. Answer (3)

44. Answer (4)

45. Answer (3)

No. of molecules in 1 gm NH_3 is $\frac{1}{17} \times N_A$ No. of molecules in 1 gm N_2 is $\frac{1}{28} \times N_A$

46. Answer (2)

Radius of n^{th} shell = $r_0 n^2$

$$\Rightarrow r_0(n+1)^2 - r_0(n-1)^2 = 2r_0 n^2$$

$$\Rightarrow (n+1+n-1)(n+1-n+1) = 2n^2$$

$$\Rightarrow 2n \times 2 = 2n^2$$

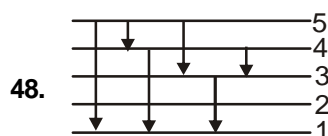
$$\Rightarrow \boxed{n=2}$$

$$47. \frac{1}{\lambda} = 1.1 \times 10^7 \left[\frac{1}{3^2} - \frac{1}{n^2} \right]$$

$$\Rightarrow v = 3 \times 10^8 \times 1.1 \times 10^7 \left[\frac{1}{9} - \frac{1}{n^2} \right]$$

Putting the values of n from the options only 5 satisfies the equation.

Hence answer is (5).



Total radiations are = 6.

49. Number of spherical nodes = $n - l - 1$.

50.

[MATHEMATICS]

51. Answer (3)

$$\begin{aligned} &= \left(\sin \frac{\pi}{14} \cdot \sin \frac{3\pi}{14} \cdot \sin \frac{5\pi}{14} \right)^2 \\ &= \left(\cos \frac{\pi}{7} \cdot \cos \frac{2\pi}{7} \cdot \cos \frac{4\pi}{7} \right)^2 \\ &= \left(\frac{\sin \frac{8\pi}{7}}{8 \sin \frac{\pi}{7}} \right)^2 = \frac{1}{64} \end{aligned}$$

52. Answer (4)

$$\alpha + \beta + \gamma = 1$$

$$\beta = \frac{1}{3}$$

$$\alpha\beta + \beta\gamma + \alpha\gamma = 3p \quad \Rightarrow \quad \beta(\alpha + \gamma) + \alpha\gamma = 3p$$

$$3p = \frac{1}{3} \times \frac{2}{3} + \alpha\gamma$$

$$3p = \frac{2}{9} + \left(\frac{1}{3} - d \right) \left(\frac{1}{3} + d \right) = \frac{1}{3} - d^2$$

$$p = \frac{1}{9} - \frac{1}{3}d^2 \quad \Rightarrow \quad p_{\max} = \frac{1}{9}$$

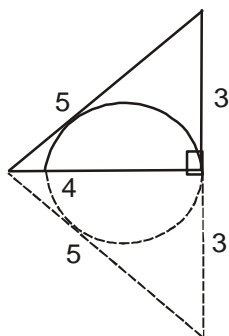
53. Answer (2)

$$\frac{x}{x+6} - \frac{1}{x} \leq 0$$

$$\frac{x^2 - x - 6}{x(x+6)} \leq 0 \quad \Rightarrow \quad \frac{(x-3)(x+2)}{x(x+6)} \leq 0$$

$$x \in (-6, -2] \cup (0, 3]$$

54. Answer (4)



$$\text{Radius of incircle} = \frac{\Delta}{s}$$

$$\begin{aligned} &= \frac{\frac{1}{2} \times 4 \times 6}{\frac{1}{2} \times (5 + 5 + 6)} = \frac{3}{2} \end{aligned}$$

$$20r - 23 = 7$$

55. Answer (1)

$$\sec \theta = m \text{ and } \tan \theta = n, \text{ then } \frac{1}{m} \left[(m+n) + \frac{1}{(m+n)} \right]$$

$$\frac{1}{\sec \theta} \left[(\sec \theta + \tan \theta) + \frac{1}{(\sec \theta + \tan \theta)} \right]$$

$$\cos \theta \left[\frac{1}{(\sec \theta - \tan \theta)} + \frac{1}{\sec \theta + \tan \theta} \right]$$

$$\cos \theta \left[\frac{\sec \theta + \tan \theta + \sec \theta - \tan \theta}{\sec^2 \theta - \tan^2 \theta} \right] = 2$$

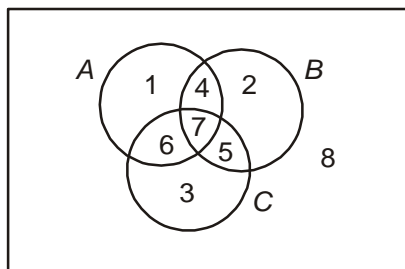
56. Answer (4)

No. of one to one functions

$$= 6 \times 5 \times 4 \times 3$$

$$= 360$$

57. Answer (4)



$$A - B = 1 + 6$$

$$B - C = 2 + 4$$

$$C - A = 3 + 5$$

$$(A - B) \cup (B - C) \cup (C - A) = 1 + 2 + 3 + 4 + 5 + 6$$

$$= (A \cup B \cup C) - (A \cap B \cap C)$$

58. $(3\sin \theta + 5\cos \theta)^2 + (5\sin \theta - 3\cos \theta)^2 = 34$

$$\Rightarrow 25 + (5\sin \theta - 3\cos \theta)^2 = 34$$

$$|5\sin \theta - 3\cos \theta| = 3.$$

Hence (B) is the correct answer.

59. $2 \sin x - \cos 2x = 2(\sin^2 x + \sin x) - 1$

$$= 2 \left[\left(\sin x + \frac{1}{2} \right)^2 - \frac{1}{4} \right] - 1$$

$$= 2 \left(\sin x + \frac{1}{2} \right)^2 - \frac{3}{2} \geq -\frac{3}{2}$$

$$\Rightarrow 2 \sin x - \cos 2x \geq -3/2$$

Hence (A), are the correct answers.

60. The given equation may be written as $8^{(1+|\cos x|+|\cos^2 x|+|\cos^3 x|+\dots+\infty)} = 8^2$

$$\Rightarrow 1 + |\cos x| + |\cos^2 x| + |\cos^3 x| + \dots + \infty = 2$$

As we have $-\pi < x < \pi, x \neq 0$, we have $|\cos x| < 1$

$$\text{Hence } \frac{1}{1-|\cos x|} = 2$$

$$\Rightarrow |\cos x| = \frac{1}{2}$$

$$\therefore \text{ values of } x \text{ in } (-\pi, \pi) \text{ for which } \cos x = \pm \frac{1}{2} \text{ are } \pm \frac{\pi}{3}, \frac{2\pi}{3}.$$

Hence (A) are the correct answer.

61. As the coefficients are real and one root is $2+i$, therefore, another root is $2-i$ (conjugate of $2+i$). Let the third root be α then sum of the roots = $2+i+2-i+\alpha$

$$\Rightarrow -(-5) = 4 + \alpha \Rightarrow \alpha = 1$$

So, the other two roots are $2-i$ and 1.

62. We have $x^2 + px + (1-p) = 0$ (i)

$$(1-p)^2 + p(1-p) + (1-p) = 0$$

$$(1-p)[1-p+p+1] = 0; p = 1$$

Put $p = 1$ in equation (i),

$$x^2 + x = 0 \Rightarrow x(x+1) = 0 \text{ i.e., } x = 0 = -1.$$

63. $y = \sqrt{\frac{(x+1)(x-3)}{(x-2)}}$

Here x cannot be 2.

\Rightarrow Either both N^r and D^r are positive

$$x \geq -1, x \geq 3 \text{ and } x > 2 \Rightarrow x \geq 3 \quad \dots(i)$$

Or N^r is negative and D^r is negative

$$x \geq -1 \text{ and } x < 2 \Rightarrow -1 \leq x < 2 \quad \dots(ii)$$

From (i) and (ii), $-1 \leq x < 2$ or $x \geq 3$.

64. C

65. $\sin \theta = \frac{1}{2} \Rightarrow \theta = \frac{\pi}{6}$

$$\cos \phi = \frac{1}{3} \Rightarrow \frac{\pi}{3} < \phi < \frac{\pi}{2}. \text{ Thus, } \frac{\pi}{2} < (\theta + \phi) < \frac{2\pi}{3}.$$

66. If $f(x) = \cos \sqrt{x}$, then $f(x)$ is not a periodic function.

67. Given, $(\cos x + \sin x)^2 + k \sin x \cos x - 1 = 0, \forall x$

$$\Rightarrow \cos^2 x + \sin^2 x + 2 \cos x \sin x + k \sin x \cos x - 1 = 0, \forall x$$

$$\Rightarrow (k+2) \cos x \sin x = 0, \forall x \Rightarrow k+2 = 0 \Rightarrow k = -2.$$

68. B

69. D

70. $n(P) = 25\%, n(C) = 15\%$

$$n(P^c \cap C^c) = 65\%, n(P \cap C) = 2000$$

$$\text{Since, } n(P^c \cap C^c) = 65\%$$

$$\therefore n(P \cup C)^c = 65\% \text{ and } n(P \cup C) = 35\%$$

$$\text{Now, } n(P \cup C) = n(P) + n(C) - n(P \cap C)$$

$$35 = 25 + 15 - n(P \cap C)$$

$$\therefore n(P \cap C) = 40 - 35 = 5. \text{ Thus } n(P \cap C) = 5\%$$

$$\text{But } n(P \cap C) = 2000$$

$$\therefore \text{ Total number of families} = \frac{2000 \times 100}{5} = 40,000$$

$$\text{Since, } n(P \cup C) = 35\%$$

$$\text{and total number of families} = 40,000$$

$$\text{and } n(P \cap C) = 5\%. \therefore (2) \text{ and } (3) \text{ are correct.}$$

71. Let the roots are α and β

$$\text{so, } \alpha^3 + \beta^3 = (\alpha + \beta)^3 - 3\alpha\beta(\alpha + \beta)$$

$$= (a-2)^3 - 3(a-3)(a-2)$$

$$= a^3 - 9a^2 + 27a - 26 = (a-3)^3 + 1$$

It assumes the least value, if $(a-3)^3 = 0$.

$$\therefore a = 3.$$

72. Given, $\tan x + \sec x = 2 \cos x$ (i)
 $\Rightarrow (\sin x + 1) = 2 \cos^2 x$
 $\Rightarrow (\sin x + 1) = 2(1 - \sin x)(1 + \sin x)$
 $\Rightarrow (1 + \sin x)[2(1 - \sin x) - 1] = 0 \Rightarrow 2(1 - \sin x) - 1 = 0$
 [$\because \sin x \neq -1$ otherwise $\cos x = 0$ and $\tan x, \sec x$ will be undefined]
 $\Rightarrow \sin x = \frac{1}{2} \Rightarrow x = \frac{\pi}{6}, \frac{5\pi}{6}$ in $(0, 2\pi)$.

73. $\sin^3 x \sin 3x = \frac{1}{4}(3 \sin x - \sin 3x) \sin 3x$
 $= \frac{3}{8} \cdot 2 \sin x \sin 3x - \frac{1}{8} \cdot 2 \sin^2 3x$
 $= \frac{3}{8}(\cos 2x - \cos 4x) - \frac{1}{8}(1 - \cos 6x)$
 $= -\frac{1}{8} + \frac{3}{8} \cos 2x - \frac{3}{8} \cos 4x + \frac{1}{8} \cos 6x$ (i)
 and $\sum_{m=0}^n c_m \cos mx = c_0 + c_1 \cos x + c_2 \cos 2x$
 $+ c_3 \cos 3x + \dots + c_n \cos nx$ (ii)
 Comparing both sides of (i) and (ii), we get $n = 6$.

74. Since $\sin x + \sin^2 x = 1$,
 $\Rightarrow \sin x = 1 - \sin^2 x = \cos^2 x$ (i)
 The given expression is
 $= \cos^6 x (\cos^6 x + 3 \cos^4 x + 3 \cos^2 x + 1) - 1$
 $= \cos^6 x (\cos^2 x + 1)^3 - 1$, ($\because \sin x = \cos^2 x$)
 $= (\sin^2 x + \sin x)^3 - 1 = 1 - 1 = 0$.

75. Since $A \subseteq B$, $\therefore A \cap B = A$
 $\therefore n(A \cap B) = n(A) = 3$.